

Flow estimation around arbitrary geometries by thermodynamics-informed neural networks

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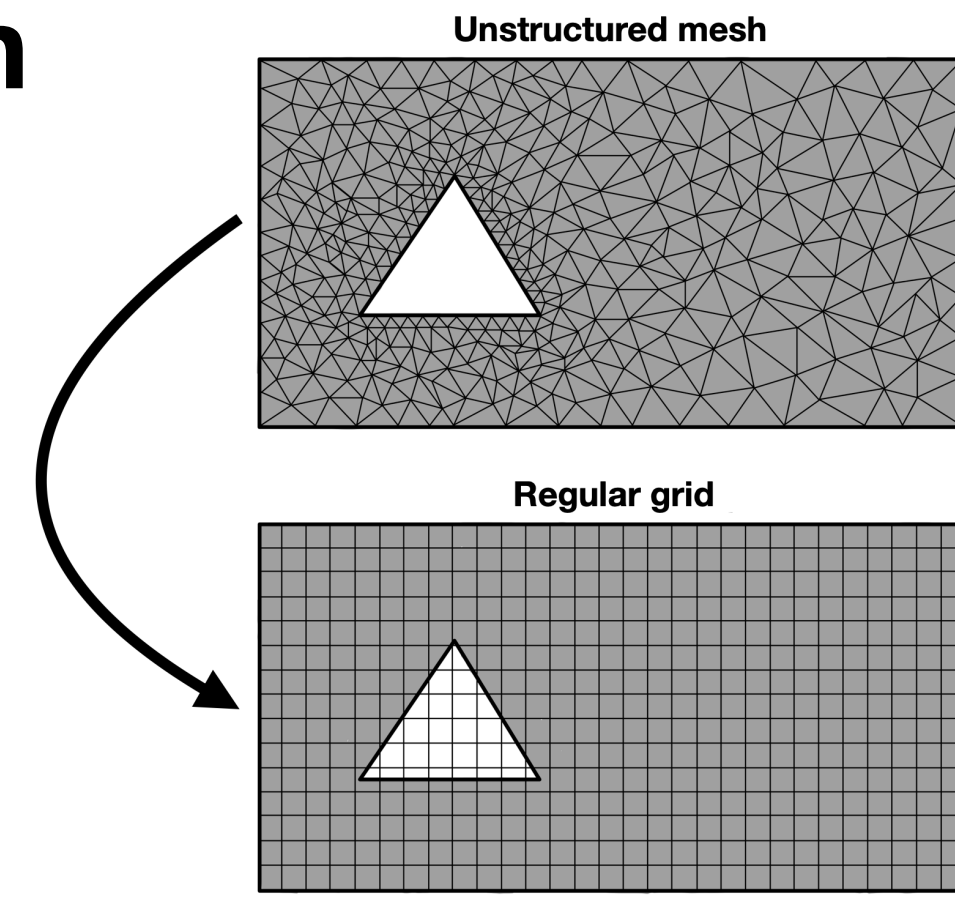
INTRODUCTION

- Complex dynamic systems → High computational cost
- Digital twins, AR, VR: need for real-time predictions
- Machine learning approaches
 - + Very fast predictions
- Lack of physics
- Solution: deep learning + physics guidance

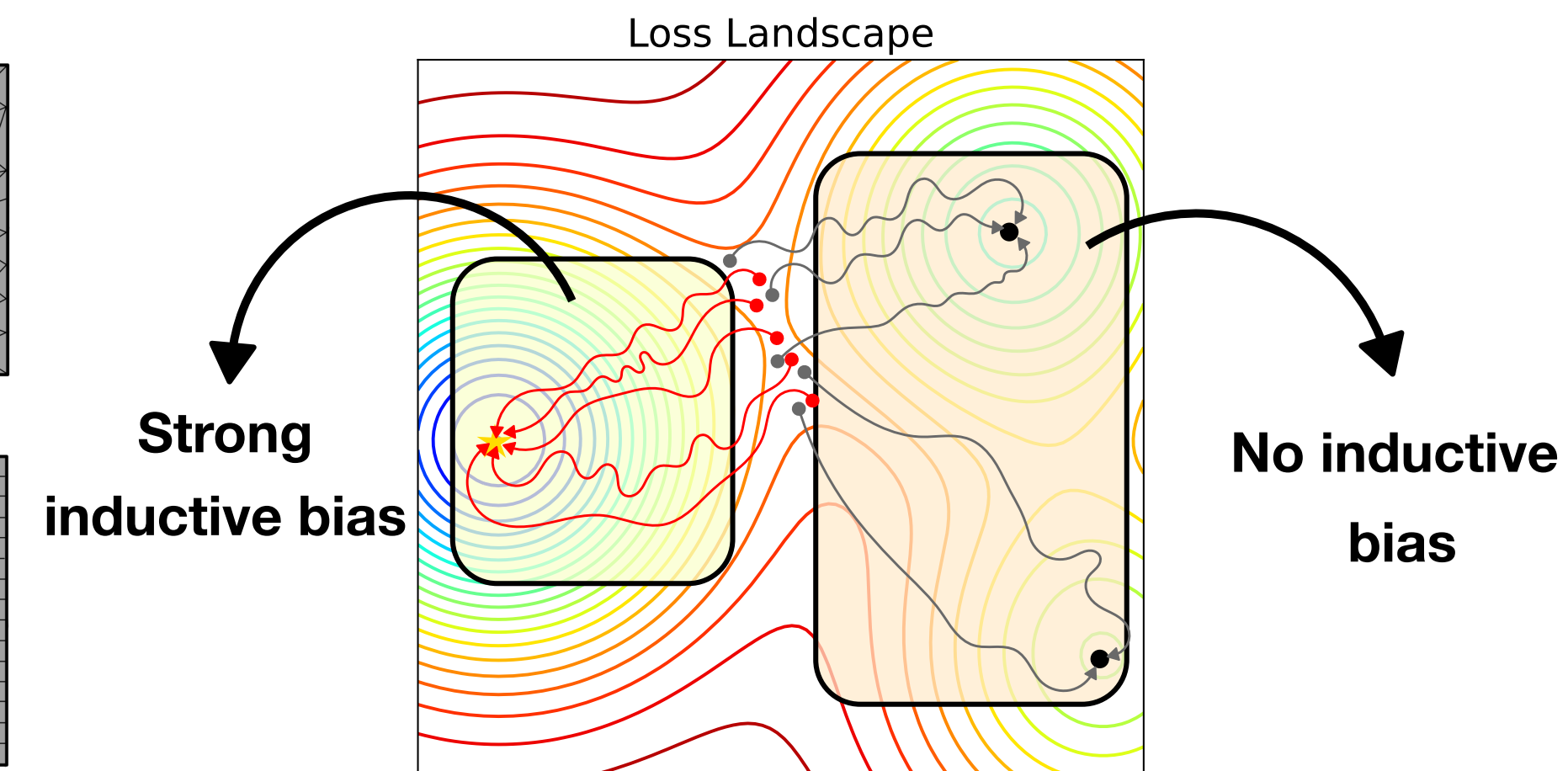
METHODS

Database Generation

- Unsteady flow over a 2D primitive geometries
- Simulations run in OpenFOAM¹
- Post-processing:
 - Unstructured mesh to grid



Inductive Biases



Deep Learning Framework

1 AAE - Adversarial Autoencoder²

- Learns a low dimensional manifold

2 SPNN - Structure Preserving Neural Network³

- Predicts the dynamical evolution of the system
- Applies the metriplectic bias - GENERIC Formalism

General Equation for Non-Equilibrium
Reversible-Irreversible Coupling (GENERIC)^{4,5}

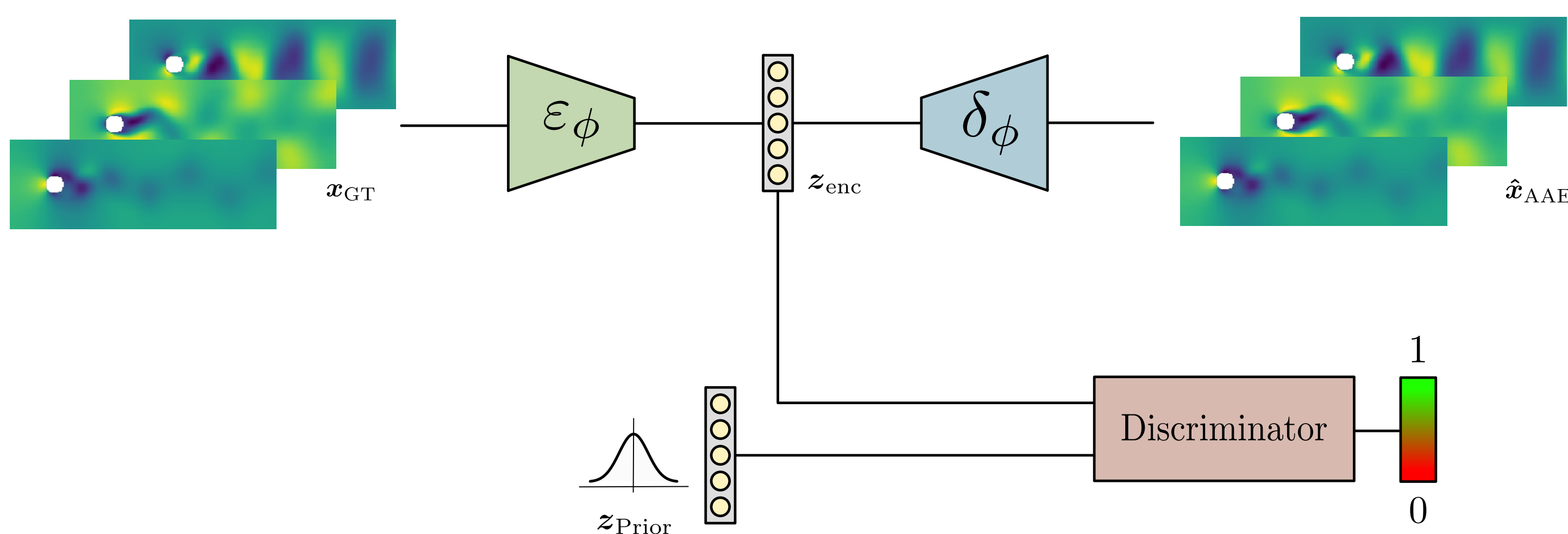
$$\frac{dz}{dt} = \mathbf{L} \frac{\partial E}{\partial \mathbf{z}} + \mathbf{M} \frac{\partial S}{\partial \mathbf{z}}$$

Symplectic manifold → Metriplectic manifold⁶

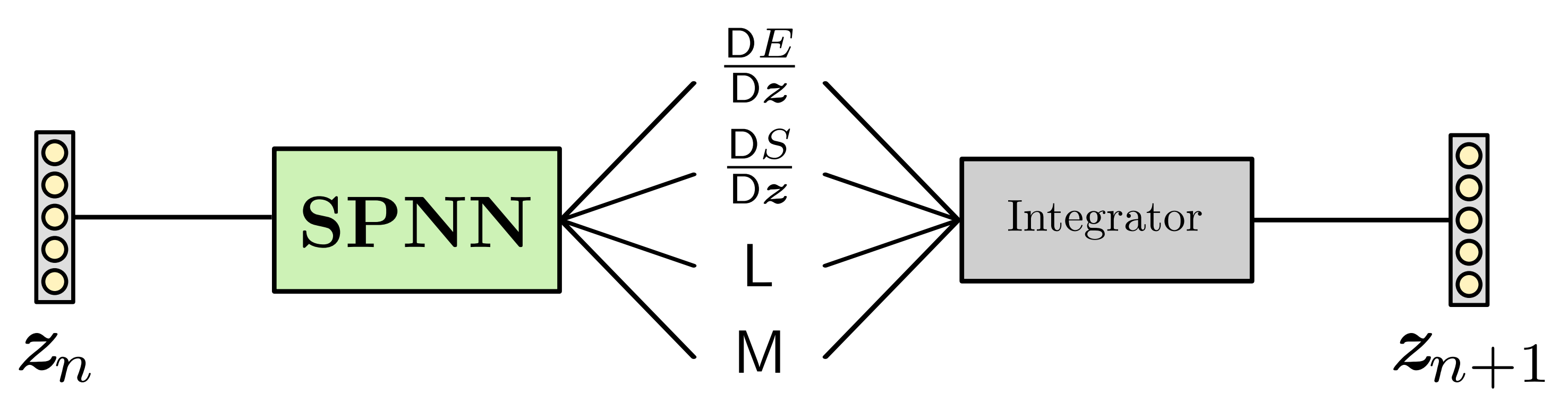
$$\begin{cases} \mathbf{L} \frac{\partial S}{\partial \mathbf{z}} = 0 \\ \mathbf{M} \frac{\partial E}{\partial \mathbf{z}} = 0 \end{cases} \Rightarrow \begin{cases} \frac{dE}{dt} = 0 \\ \frac{dS}{dt} \geq 0 \end{cases}$$

Degeneracy conditions Fullfills 1st and 2nd laws of Thermodynamics

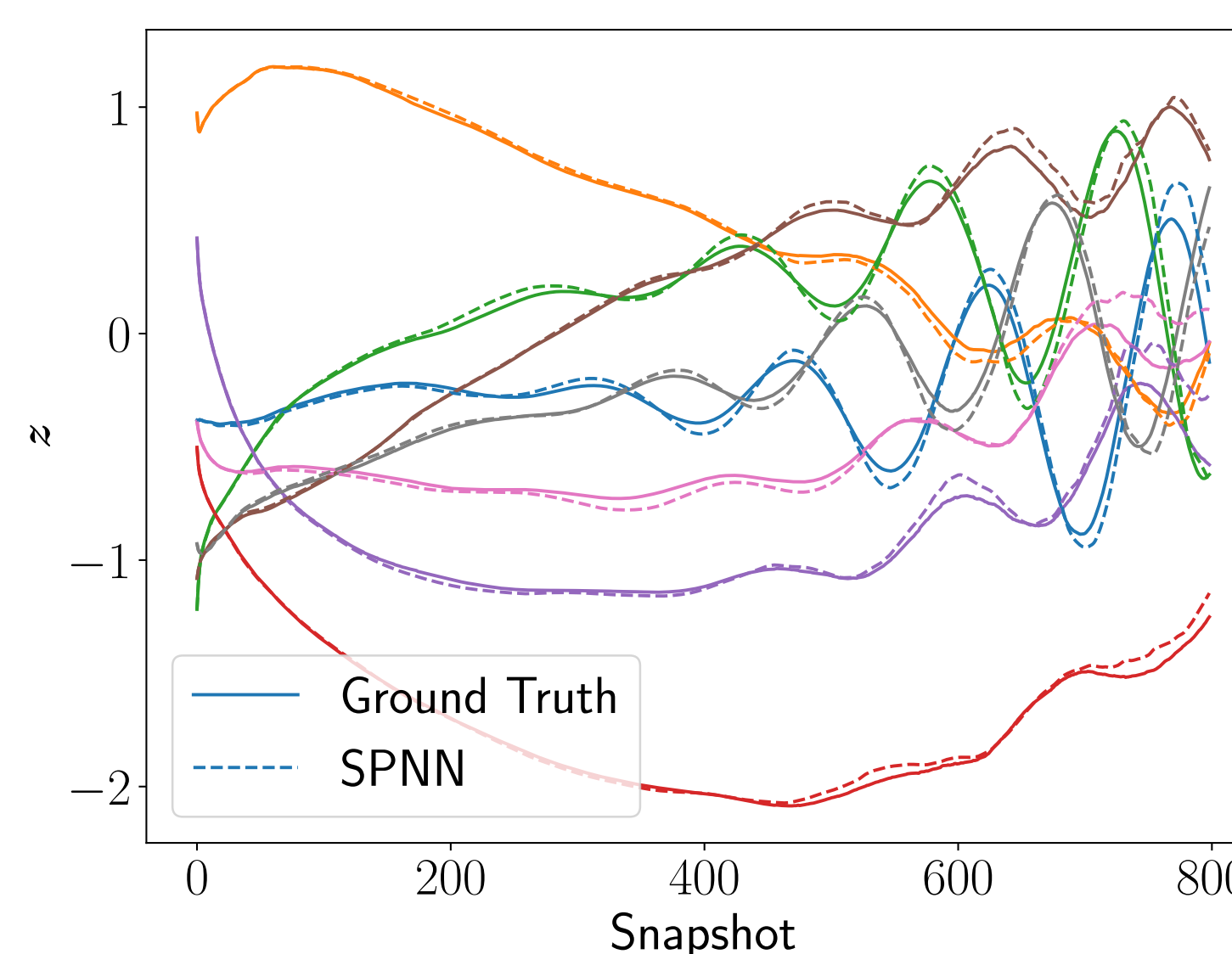
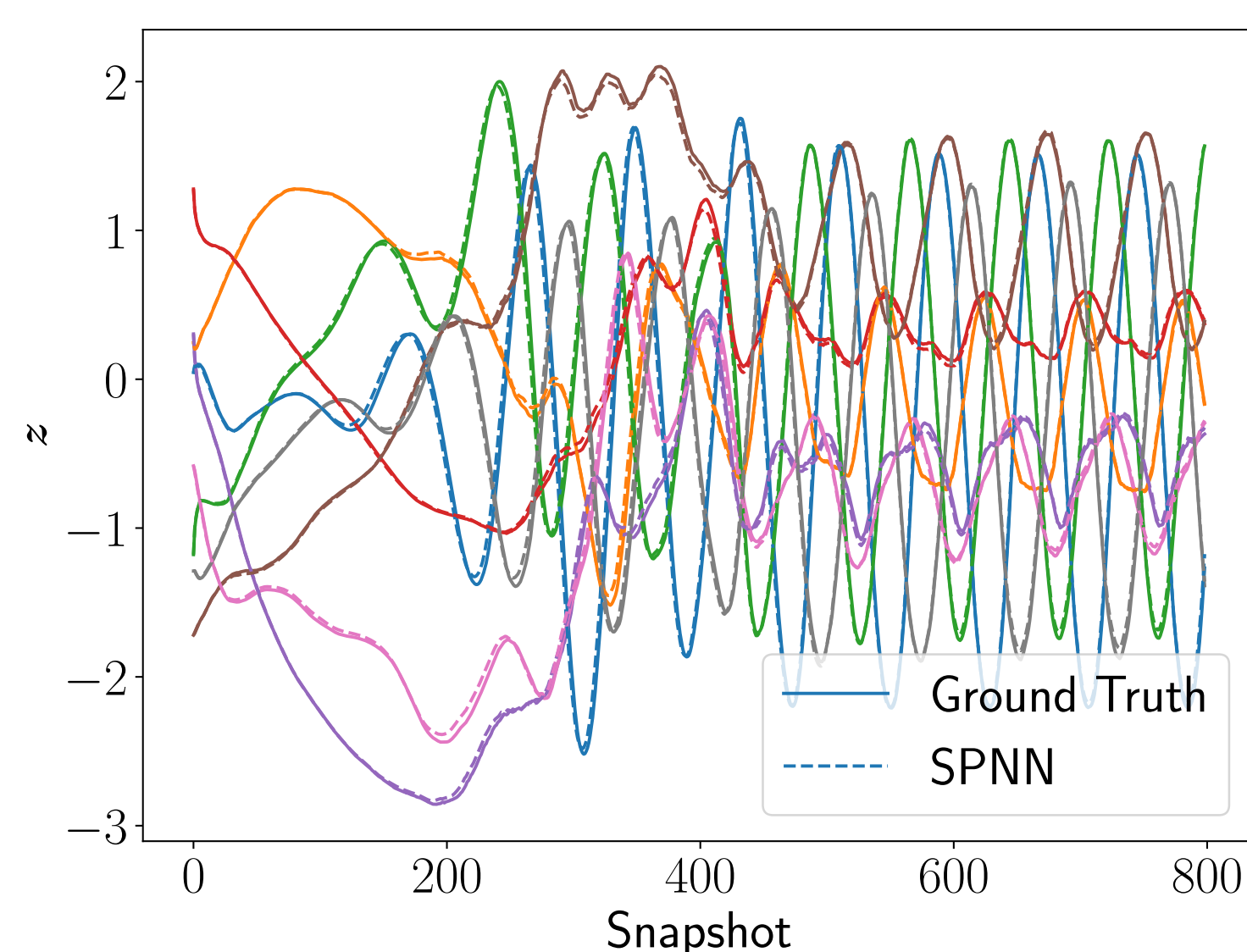
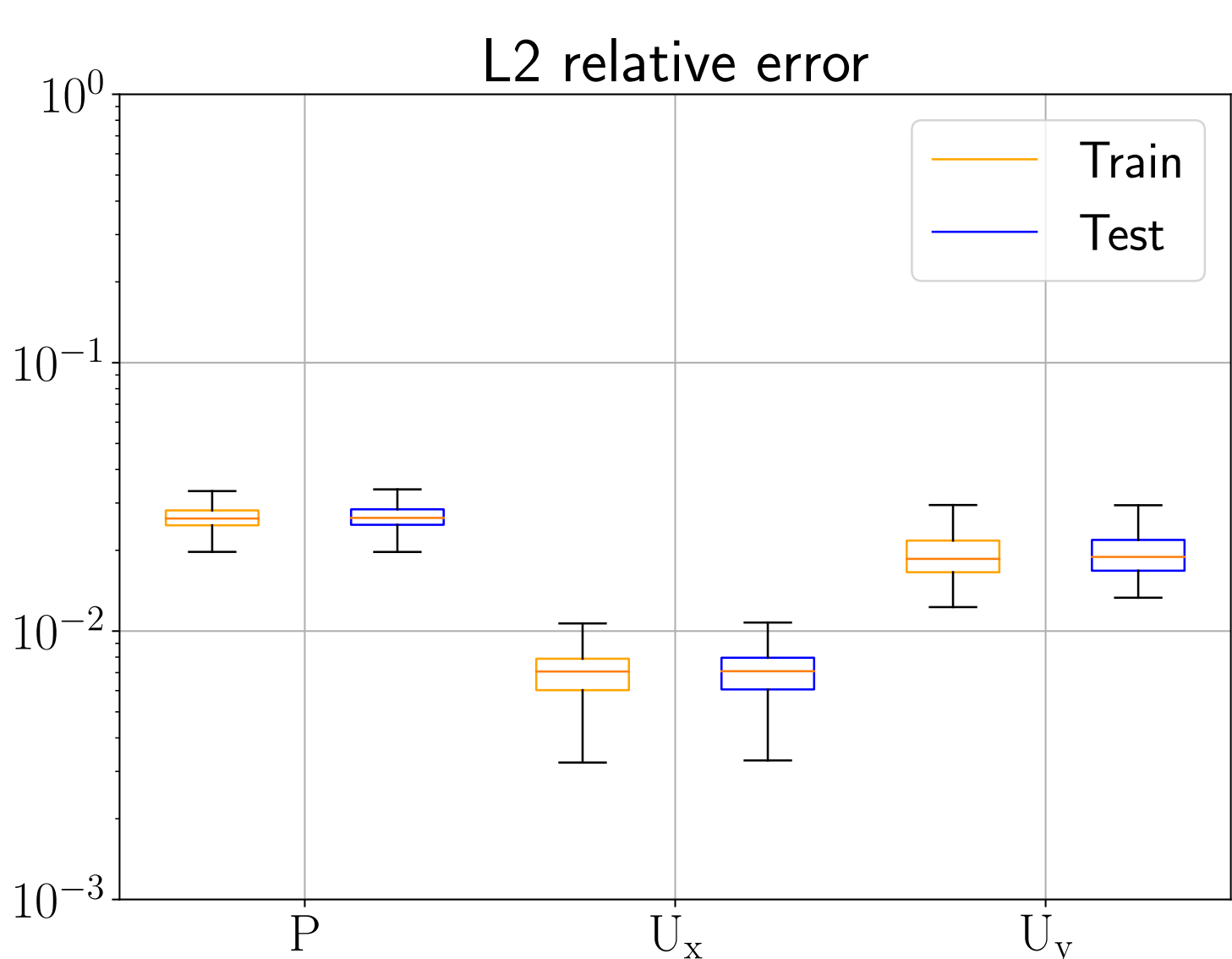
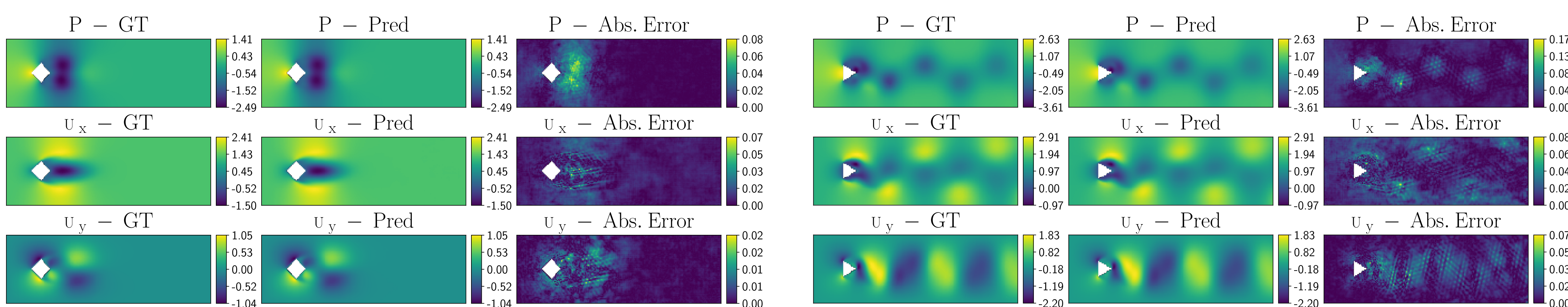
1 Adversarial Autoencoder



2 Structure Preserving Neural Network



RESULTS



VIDEOS HERE!



CONCLUSIONS

- Successful codification of the flow achieved by the AAE
- Thermodynamics-based biases help to improve robustness and generalization

FUTURE WORK

- Apply metriplectic and geometric biases together - GNN



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References

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